

Fall 2008, Hitotsubashi University  
**Monetary Economics 1**  
 (Corporate Finance)

LECTURE 3  
**Valuation of Risky Investment  
 Project and Capital structure**

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Use CAPM to determine risk-adjusted discount.

- CAPM: A Primer
- $E[r_i] - r_f = \beta_i (E[r_M] - r_f)$ 
  - $r_i$ : return of asset  $i$ ;  $r_f$ : return of riskless asset
  - $r_M$ : return of market portfolio
  - $\beta_i = \text{Cov}(r_i, r_M) / \text{Var}(r_M)$
  - Please do read about the derivation of CAPM by yourself.

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## Interpretation of CAPM

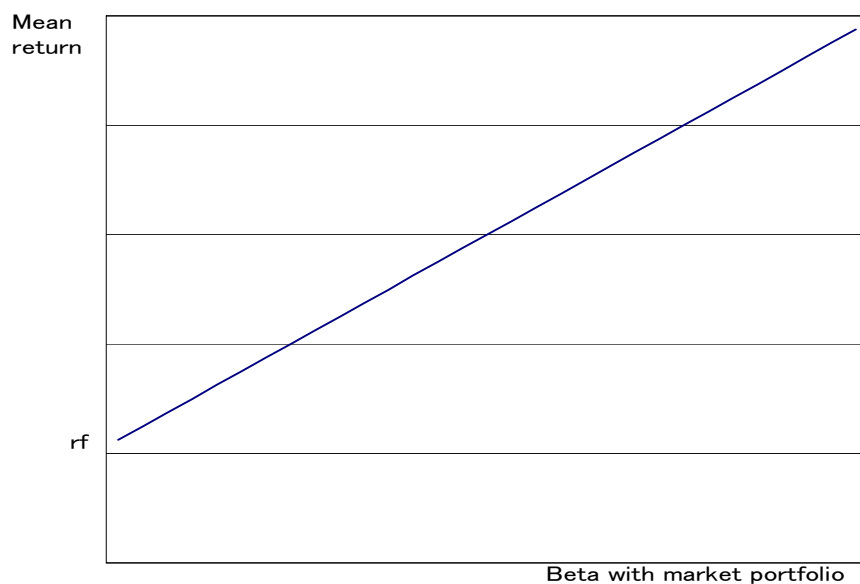
$$E[r_i] - r_f = \beta_i (E[r_M] - r_f)$$

- Relation between expected excess returns of asset  $i$  and market portfolio.
- Higher the covariance with market portfolio, higher the expected excess return.
- What is relevant for valuation is covariance risk, not variance.
- If correlation is zero, no matter how large the variance was,  $E[r_i] - r_f = 0$ .

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## Implementation of CAPM

- $E[r_i] - r_f = \beta_i (E[r_M] - r_f) + \varepsilon_i$
- Regression of “excess return of asset  $i$ ” on “excess return of market portfolio”
  - No constant term.
  - $Y_i = \beta_i X_M + e_i$

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## Why is the market portfolio a benchmark?

- By investing to many different assets, one can diversify risks.
- The risks that will disappear by diversification are not be priced, i.e. risk premium is zero.
- Only covariance with most diversified portfolio matters.
- Most diversified portfolio = the market portfolio

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## A digression: What is risk premium?

- Riskless asset:  $r_f$
- Risky asset:  $r_i$        $E[r_i], \text{Var}(r_i)$
- $\text{Var}(r_i) > 0 \rightarrow r_i > r_f$
- The condition that both riskless and risky assets are invested:  

$$U(W \cdot r_f) = E[U(W \cdot r_i)]$$
- Let “ $q$ ” be the premium required for a risky asset over riskless asset return so that the condition above is satisfied:  

$$E[r_i] = r_f + q$$

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## Determination of risk premium by CAPM

- Volatility of security  $i$   
 $= \beta_i \times \text{market risk} + \text{“idiosyncratic risk”}$
- $E[r_i] - r_f = \text{Risk premium of security } i$   
 $= \beta_i \times \text{“risk premium of market risk”}$   
 $= \beta_i (E[r_M] - r_f)$
- The project should be invested if and only if:  

$$E[r_{\text{project}}] \geq E[r_{\text{comp.}}]$$

$$= r_f + \beta_{\text{comp.}} (E[r_M] - r_f)$$

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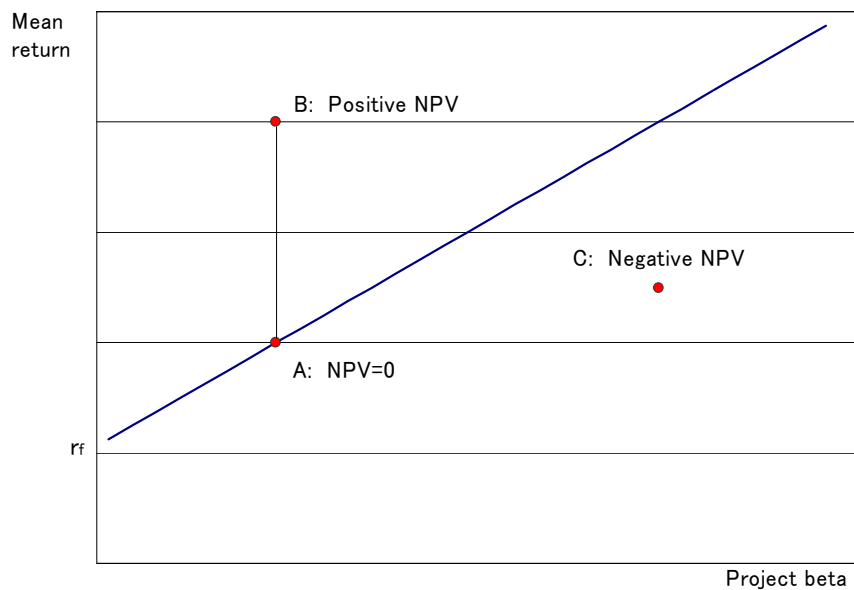
## Graphical expression

- If the project was located on or at the left-side of SML, the investment project should be accepted.
- Given the estimated project beta, expected return is sufficiently large.

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## Risk-adjusted discount rate

- Forecast future cash flow:  $E[CF]$
- Estimate the project's beta:  $\beta$
- Use  $\beta$  to calculate risk premium
- Discount forecasted future cash flow  $E[CF]$  by risk-adjusted discount rate

$$PV = \frac{E[CF]}{1 + r_f + \beta(R_M - r_f)}$$

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## Important points

- Tracking portfolio approach is implicit in risk-adjusted discount rate method.
- We assumed full equity finance, i.e. no leverage, in the discussions so far.

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## The effect of leverage

- In general comparison firms are financed by both equities and debts (leverage).
- In such a case, beta of comparison firm's business is different from the firm's equity beta.
- We still make an important simplifying assumption:
  - Modigliani=Miller's theorem (MM theorem) is satisfied so that the financial structure does not affect the firm's value.

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## Equity vs debt

- Cost of debt financing = interest rate payment on debt
- "Firm's value" minus "firm's debt value"  
= Value of firm's equities
- Cost of equity financing: Equity's expected return (interest rate + risk premium)
- Risk premium is required so that equity holders will bear the volatility of stock prices.

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## Calculating WACC : simple case

- WACC=Weighted average cost of capital
- “Cost of equity financing” x “the amount financed by equities”
- “Cost of debt financing” x “the amount financed by debts”
- Summing them up, then divide by total amount = WACC

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## Algebraic derivation (1)

- The firm's total value:  $V$
- The firm's future cash flow:  $CF$
- The firm's cost of capital (= expected return from its business):  $r_{Firm}$
- The firm's total value (assume annuity):  
$$V = CF / r_{Firm}$$
- Capital structure of the firm:  $V = E + D$
- $r_{Firm} = CF / V = CF / (E + D)$

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## Algebraic derivation (2)

- Equity holders' future cash flow:  $CF - r_{Debt}D$
- So,  $E = (CF - r_{Debt}D) / r_{Stock}$
- $CF = r_{Stock}E + r_{Debt}D$ 
  - LHS: Future cash flow from the firm's business
  - RHS: The amount required to payout for stock holders and debt holders.

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## WACC: general formula

- Divide both LHS and RHS by  $V = E + D$
- Firm's cost of capital =  
 "Ratio of equity finance" x "Equity cost of capital"  
 + "Ratio of debt finance" x "interest rate on debt"

$$r_{Firm} = \left( \frac{E}{E + D} \right) r_{Stock} + \left( \frac{D}{E + D} \right) r_{Debt}$$

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## The role of MM theorem

- We assumed MM is satisfied:
  - MM says the firm's value is not affected by its financial structure.
  - So  $r_{Firm}$  is constant.
- $r_{Stock}$  and  $r_{Debt}$  are determined in market and can be observed.
- We should use  $r_{Firm}$  to evaluate investment project, but  $r_{Firm}$  cannot be observed directly.